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Characterization of Poly(1,4-phenyleneterephthalamide) in Concentrated Sulfuric Acid. 4. Dilute and Semidilute Solution Regimes

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ABSTRACT: From our analysis of the concentration and angular dependence of the static and dynamic properties (excess Rayleigh ratio $\Delta R_{\rm vv}$, radius of gyration $R_{\rm g}$, hydrodynamic radius $R_{\rm h}$, characteristic decay time Γ^{-1} , and second virial coefficients A_2 and $k_{\rm d}$) of poly(1,4-phenyleneterephthalamide) (PPTA) in concentrated sulfuric acid (with and without the addition of a small amount of K_2SO_4), we have been able to examine the crossover behavior from the dilute to the semidilute solution regime for a rodlike polymer in solution. According to the scaling theory, the overlap concentration C^* for random coils is $\sim M/(N_A R_g^3)$, with M and N_A being the molecular weight and the Avogadro number, respectively. For rod macromolecules, $M/(N_A L^3) \lesssim C^*$. From semidilute to concentrated solution, an additional crossover behavior takes place. For rod macromolecules, $C^{**} \lesssim M/(N_A dL^2)$, with d and L being the rod diameter and length, respectively. In plots of $\lim_{K\to 0} \left[\Delta R_{\rm vv}/(HC)\right]$ vs. concentration, the concentration $C_{\rm m}$ at which $\lim_{K\to 0} \left[\Delta R_{\rm vv}/(HC)\right]$ shows a minimum can be represented by a modified Doi–Edwards inequality: $C_{\rm m} \lesssim M/(N_A d^*L^*2)$, with d^* and L^* being an effective diameter and an effective length of the macromolecule. K is the magnitude of the momentum transfer vector, ΔR is the excess Rayleigh ratio, and H is an optical constant. In a plot of $\log \left[M_{\rm app}(HC/\Delta R_{\rm vv}) - 1\right]$ vs. $\log \left(C/C_{\rm m}\right)$, where $M_{\rm app}$ is the apparent molecular weight, the slope is equal to 1 for $C < C_{\rm m}$ as de Gennes has predicted. The correlation length corresponding to the apparent root mean square radius of gyration at finite concentration was found to increase sharply above $C_{\rm m}$, similar to the observation made by Burchard for aqueous poly(vinylpyrrolidone) solutions in the semidilute solution region.

I. Introduction

In previous papers, $^{1-3}$ we have characterized the dilute solution properties of poly(1,4-phenyleneterephthalamide) (PPTA) in concentrated sulfuric acid (with and without a small amount of K_2SO_4) using light scattering (LS) intensity and line-width measurements. We have been able to estimate the molecular weight dependences of intrinsic viscosity, of radius of gyration $\langle R_g \rangle_z^{1/2}$, and of translational diffusion coefficient \hat{D}_z as well as the persistence length ρ (~290 Å) of PPTA in concentrated sulfuric acid. In addition, we have been able to estimate the molecular weight distributions of unfractionated PPTA samples³ and to devise a simple calibration technique capable of monitoring molecular weight as well as molecular weight polydispersity index changes.⁴ In this article, we present the crossover behavior for PPTA in concentrated sulfuric acid,

with and without the addition of a small amount of $\rm K_2SO_4$. Rodlike polymers are prone to interchain association. Therefore, at higher solution concentrations interchain interactions may play an important role in the crossover behavior from the dilute to the semidilute solution regime. The behavior of the threshold concentration from dilute to semidilute solution is controlled by chain rigidity as well as molecular size. All experiments, including sample preparation and instrumentation, follow the same procedures as described in detail elsewhere. 2,3

II. Dilute Solution Properties

Dynamic light scattering (LS) in combination with static light scattering intensity measurements has been shown to be a valuable approach to deduce information about macromolecular size, shape, molecular weight distribution,

and interactions. In static LS measurements, the excess Rayleigh ratio ΔR (ΔR_{vv} or ΔR_{hv} , vertical and horizontal components of excess Rayleigh ratio using vertically polarized incident light) and the weight-average molecular weight $M_{\rm w}$ are related according to the expressions

$$HC/\Delta R_{vv}(C,K=0) = 1/M_{app} + 2A_2C$$
 (1)

$$HC/\Delta R_{vv}(C=0,K) = (1/M_{app})(1 + \langle R_g^2 \rangle_{app} K^2/3 + ...)$$
 (2)

$$M_{\rm app} = M_{\rm w}(1 + 4\delta^2/5) \tag{3}$$

$$\langle R_g^2 \rangle_{\text{app}} = \langle R_g^2 \rangle [(1 - 4\delta/5 + 4\delta^2/7)/(1 + 4\delta/5)]$$
 (4)

where $H = [4\pi^2 n^2/(N_A \lambda_0^4)](\partial n/\partial C)^2$ and $K = (4\pi n/\lambda_0)(\sin n/\alpha)$ $(\theta/2)$). The molecular anisotropy δ can be calculated from the ratio of ΔR_{vv} and ΔR_{hv} at zero scattering angle and infinite dilution by the relation $\Delta R_{vv}^{0}/\Delta R_{hv}^{0} = 3\delta^{2}/(5 +$ $4\delta^2$), where the superscript zero denotes extrapolation of the excess Rayleigh ratio to zero scattering angle at infinite dilution.

In the self-beating mode, the intensity time correlation function $G^{(2)}(t)$ is related to the first-order electric field time correlation function $g^{(1)}(t)$ by

$$G^{(2)}(t) = A(1 + b|g^{(1)}(t)|^2)$$
 (5)

where A is the background and the coherence factor, b, is assumed to be an adjustable fitting parameter. In the cumulant expansion

$$\ln g^{(1)}(t) = -\bar{\Gamma}t + \sum (-1)^{i} \frac{\mu_{i}t^{i}}{i!}$$
 (6)

At small scattering angles, the first cumulant $\bar{\Gamma}$ is related to the average translational diffusion coefficient \bar{D} by

$$\lim_{K \to 0} \bar{\Gamma} = K^2 \bar{D} \tag{7}$$

with

$$\bar{D} = \bar{D}_z^{\ 0} (1 + k_d C) \tag{8}$$

At larger scattering angles, eq 7 is modified to yield

$$\bar{\Gamma}/K^2 \simeq \bar{D}(1 + f\langle R_g^2(C) \rangle_{app} K^2)$$
 (9)

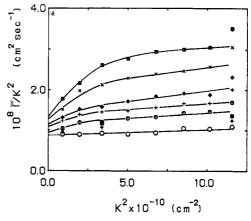
which shows a similar concentration and angular dependence as those of eq 1 and 2. Thus, Burchard and Eisele⁶ suggested a modified Zimm plot using $\bar{\Gamma}/K^2$ according to eq 8 and 9. In our case, the angular dependence of $\bar{\Gamma}/K^2$ vs. K^2 for solutions of PPTA in concentrated sulfuric acid without and with the addition of a small amount salt (K₂SO₄), as shown respectively in parts a and b of Figure 1, suggests a noticeable deviation from only the K^4 -order expansion of eq 9. Thus, for PPTA solutions, we must be particularly careful in trying to obtain reliable extrapolation results. By using a semilogarithmic relationship, as sometimes practiced in light scattering intensity data analysis, the extrapolation procedure to zero scattering angle can be improved. Thus, eq 9 is rewritten as

$$\ln (\bar{\Gamma}(0,K)/K^2) \simeq \ln \bar{D}_z^0 + \ln [1 + f(R_g^2)_{app}K^2]$$
 (10)

with $\bar{\Gamma}(0,K)$ denoting $\bar{\Gamma}(C,K)$ at infinite dilution. In our case, the mean square radius of gyration $\langle R_{\rm g}^2 \rangle \sim 10^{-11} \ {\rm cm}^2$, $K^2 \sim 10^{10} \ {\rm cm}^2$, and f < 1, so $[f \langle R_{\rm g}^2 \rangle_{\rm app} K^2]^2 < 1$. Since $\ln (1+X) = X - (1/2)X^2 + (1/3)X^3 - ...$ for $X^2 < 1$, eq 10 becomes

$$\ln \left(\bar{\Gamma}(0,K)/K^2\right) \simeq \ln \tilde{D}_z^0 + f \langle R_g^2 \rangle_{\text{app}} K^2 \tag{11}$$

Figure 2 shows a plot of $\ln (\bar{\Gamma}/K^2)$ vs. K^2 for sample 4 in 96% H_2SO_4 solutions. In Figure 2, all $\bar{\Gamma}$'s were evaluated by using the third-order cumulant fit. In comparison with those from the second-order cumulant fit, we found the



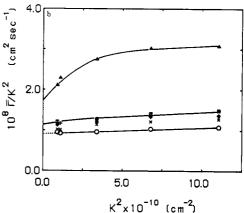


Figure 1. (a) Plots of $\bar{\Gamma}/K^2$ vs. K^2 for sample 4 (third-order cumulant fit) in 96 wt % H_2SO_4 at different concentrations: (O) C=0, (†) $C=0.40\times 10^{-3}$, (\blacksquare), $C=0.72\times 10^{-3}$, (\bigcirc) $C=1.18\times 10^{-3}$, (+) $C=2.14\times 10^{-3}$, (\blacksquare) $C=2.80\times 10^{-3}$, (×) $C=4.54\times 10^{-3}$, and (\square) $C=6.36\times 10^{-3}$ g/mL. Solid curves are freely drawn to illustrate the noticeable deviation from the K^4 -order expansion of $\bar{\Gamma}$ at finite concentrations and K values. (b) Plots of $\bar{\Gamma}/K^2$ vs. K^2 for sample 4 (third-order cumulant fit) in 96 wt % H.SO. + K^2 for sample 4 (third-order cumulant fit) in 96 wt % H_2SO_4 + 0.05 M K₂SO₄ at different concentrations: (0) C=0, (×) $C=0.60\times 10^{-3}$, (•) $C=1.04\times 10^{-3}$, (+) $C=1.30\times 10^{-3}$, (□) $C=1.70\times 10^{-3}$, and (•) = 7.68 × 10⁻³ g/mL. Solid curves are freely drawn to illustrate the noticeable deviation from the K⁴-order expansion of $\bar{\Gamma}$ at finite concentrations and K values.

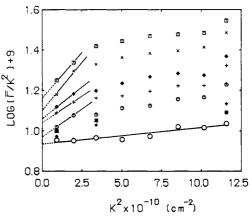


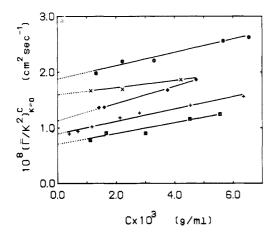
Figure 2. Plots of $\log (\bar{\Gamma}/K^2) + 9$ vs. K^2 for sample 4 in 96% $H_2 SO_4$ based on data in Figure 1a. Initial slopes are shown to illustrate the extrapolation procedure for $K \to 0$. Similar values of $\lim_{K \to 0, C \to 0} (\bar{\Gamma}/K^2)$ are obtained by using a second-order cumulant fit.

extrapolated Γ values to be in reasonable agreement, independent of the fitting procedure. The use of eq 10 and 11 instead of eq 9 is not necessary whenever $f\langle R_g^2 \rangle_{app} K^2$ < 1. In our case, we obtained similar results by either means. Values of the variance $\mu_2/\bar{\Gamma}^2$ tend to increase with

Table I
Static and Dynamic Properties of PPTA in Concentrated Sulfuric Acid with and without Added Salt

sample	solvent	$M_{\scriptscriptstyle W} imes 10^{-4}$	$ar{D_z} imes 10^8,^a \ m cm^2/s$	$R_{ m h}$, b nm	$R_{g},^c$ nm	f
5	96 wt % H ₂ SO ₄	4.83	0.72	18.2	48	0.06
$\overset{\circ}{4}$	96 wt % H ₂ SO ₄	3.84	0.88	14.9	33	0.21
3	96 wt % H ₂ SO ₄	2.27	1.13	11.5	22	0.29
2	96 wt % H ₂ SO ₄	1.59	1.59	8.2		
1	96 wt % H ₂ SO ₄	1.45	1.96	6.7		
5	96 wt % H ₂ SO ₄ + 0.05 M K ₂ SO ₄	4.26	0.74	17.6	35	0.30
4	96 wt % $H_2SO_4 + 0.05 \text{ M K}_2SO_4$	2.98	0.93	14.1	34	0.19
3	96 wt % $H_2SO_4 + 0.05 \text{ M K}_2SO_4$		0.99	13.1		
2	96 wt % $H_2SO_4 + 0.05 \text{ M K}_2SO_4$		1.57	8.3		

 ${}^a\bar{D}_z$ is the z-average diffusion coefficient with an estimated precision of a few percent. ${}^bR_{\rm h}$ is the average hydrodynamic radius, with $\bar{D}_z = k_{\rm B}T/(6\pi\eta_0 R_{\rm h})$. ${}^cR_{\rm g} \equiv \langle R_{\rm g}^2 \rangle_z^{1/2}$; $\langle R_{\rm g}^2 \rangle_{\rm app}$ can be computed according to eq 4 using δ values listed in ref 2.



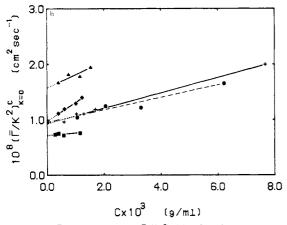


Figure 3. (a) Plots of $\lim_{K\to 0} (\bar{\Gamma}/K^2)$ (third-order cumulant fit) vs. concentration for PPTA samples in 96% H_2SO_4 : (■) sample 5; (+) sample 4; (♦) sample 3; (×) sample 2; (○) sample 1. (b) Plots of $\lim_{K\to 0} (\bar{\Gamma}/K^2)$ (third-order cumulant fit) vs. concentration for PPTA samples in 96% $H_2SO_4 + 0.05$ M K_2SO_4 : (■) sample 5; (+) sample 4; (♦) sample 3; (♠) sample 2; (●) sample 4 in 96% $H_2SO_4 + 0.005$ M K_2SO_4 .

increasing concentration and increasing scattering angle. In Figure 2 $\bar{\Gamma}/K^2$ seems to deviate from the K^2 dependence at K^2 equal to $\sim 4 \times 10^{10}$ cm⁻². Thus, values of $\bar{\Gamma}(C,K=-0)/K^2$ were evaluated from the intercepts by using the initial slope at relatively low scattering angles $K^2 < 4 \times 10^{10}$ cm⁻². Parts a and b of Figure 3 show plots of $\bar{\Gamma}(C,0)/K^2$ vs. concentration for five PPTA samples in 96% H_2SO_4 and 96% $H_2SO_4 + 0.05$ M K_2SO_4 , respectively. From a linear concentration dependence of $\bar{\Gamma}(C,0)/K^2$, we have

$$\bar{\Gamma}(C,0)/K^2 = \bar{D}_z^0 + k_d * C \tag{12}$$

with $k_{\rm d}^* = \bar{D}_z^{~0}k_{\rm d}$. $k_{\rm d} \sim 125~{\rm cm}^3/{\rm g}$ for samples 3, 4, and 5 in 96% $\rm H_2SO_4$, which is higher than those we estimated

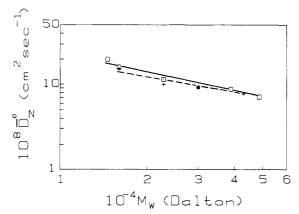


Figure 4. log-log plots of \bar{D}_z^0 vs. $M_{\rm w}$ at 30 °C, where \bar{D}_z^0 and $M_{\rm w}$ denote the z-average translational diffusion coefficient at infinite dilution and the weight-average molecular weight, respectively. Hollow rectangles, in H₂SO₄; solid line denotes $\bar{D}_z^0 = 2.72 \times 10^{-5} M_{\rm w}^{-0.77}$ cm²/s; triangle, in H₂SO₄ + 0.005 M K₂SO₄; crosses, in H₂SO₄ + 0.05 M K₂SO₄; dashed line denotes $\bar{D}_z^0 = 1.51 \times 10^{-5} M_{\rm w}^{-0.72}$ cm²/s. Note the suggested slight difference for PPTA in H₂SO₄ with and without added salt.

in paper 1.² Nevertheless, $k_{\rm d}$ does not show a strong molecular weight dependence within the molecular weight range of our studies ((2.3–4.8) × 10⁴). For the other two lower molecular weight samples, $k_{\rm d}$ was estimated to be 45 cm³/g. In fact, more experimental work should be done in order to evaluate the relatively weak molecular weight dependence of $k_{\rm d}$. Values of $\bar{D}_z^{\ 0}$ and the corresponding hydrodynamic radius $R_{\rm h}$ are listed in Table I. We used

$$R_{\rm h} = k_{\rm B} T / (6\pi \eta_0 \bar{D}_z^{\ 0}) \tag{13}$$

where $k_{\rm B}$ and η_0 are the Boltzmann constant and the solvent viscosity, respectively. The molecular weight dependence of $\bar{D}_z{}^0$ for PPTA in 96% $H_2{\rm SO}_4$ (with and without added $K_2{\rm SO}_4$) is shown in Figure 4. For PPTA in 96% $H_2{\rm SO}_4$ at 30 °C, least-squares fitting results show

$$\bar{D}_z^0 = 2.72 \times 10^{-5} M_w^{-0.77} \text{ cm}^2/\text{s}$$
 (14)

$$R_{\rm h} = 4.78 \times 10^{-10} M_{\rm w}^{0.77} \, {\rm cm}$$
 (15)

and in 96% $H_2SO_4 + 0.05 M K_2SO_4$

$$\bar{D}_z^0 = 1.51 \times 10^{-5} M_w^{-0.72} \text{ cm}^2/\text{s}$$
 (16)

$$R_{\rm h} = 8.63 \times 10^{-10} M_{\rm w}^{0.72} \, {\rm cm}$$
 (17)

In Figure 4 the slopes in 96% $\rm H_2SO_4$ and in 96% $\rm H_2SO_4$ + 0.05 M $\rm K_2SO_4$ appear to agree within experimental error limits; i.e., the values (0.77 and 0.72) are not far from \sim 0.75, which we estimated in paper 1² without careful extrapolation of $\bar{\Gamma}/K^2$ to zero scattering angle. The molecular weight dependence for the radius of gyration is shown in Figure 5. Our data suggest that $\langle R_g^2 \rangle_z^{1/2} = 9.21$

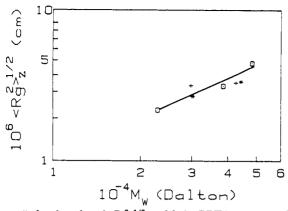


Figure 5. log-log plot of $\langle R_{\rm g}^2 \rangle^{1/2}$ vs. $M_{\rm w}$ for PPTA in 96% H₂SO₄ (O), in 96% H₂SO₄ + 0.005 M K₂SO₄ (*), and in 96% H₂SO₄ + 0.05 M K₂SO₄ (+). Solid line denotes $\langle R_{\rm g}^2 \rangle^{1/2} = 9.21 \times 10^{-10} M_{\rm w}^{0.78}$

 \times $10^{-10} M_{\rm w}^{-0.78},$ with $R_{\rm g}$ expressed in cm. An $\alpha_{R_{\rm g}}$ exponent of 0.78 for PPTA in 96% H₂SO₄ also seems to have a higher value than that for PPTA in H₂SO₄ with K₂SO₄. Perhaps the PPTA chain appears to be more rigid in H₂SO₄ than the same chain in H₂SO₄ with added salt, or perhaps some side-by-side salt association could increase the overall rigidity of the system.

Wilcoxon and Schurr⁷ presented an equation that deals with the angular dependence of $D_{app}(K) = (\bar{\Gamma}/K^2)$ for rigid

$$D_{\rm app}(K) = \bar{D}_z^0 + 2\Delta(1/3 - F(KL)) + 2L^2D_RG(KL) \quad (18)$$

where F(KL) and G(KL) are universal functions of KL and are independent of molecular weight. It should be noted that eq $\bar{9}$ describes the general $K^{\bar{2}}$ expansion of $\bar{\Gamma}/K^2$ for macromolecular solutions, irrespective of polymer shape, and is valid for random coils and semiflexible chains, as well as rigid rods, while eq 18 is valid only for rigid rods. Wilcoxon and Schurr calculated values of F(KL) and G(KL) from KL = 0 to infinity and listed the results in their Table 1 of ref 7. Thus, $D_{app}(K)$ can be calculated by using eq 18 for any thin rods for which \bar{D}_z^0 , Δ , L, and D_R are known. $\Delta (=D_{\parallel} - D_{\perp})$ is the anisotropy of the translational diffusion coefficient, with D_{\perp} and D_{\parallel} being the translational diffusion coefficients perpendicular and parallel to the rod axis, respectively. Using Broersma's relations,8 one can express the rotational diffusion coefficient $D_{\rm R}$ and other quantities:

$$D_{\parallel} = (k_{\rm B}T/2\pi\eta_{\rm 0}L)(s - r_{\parallel}) \tag{19}$$

$$D_{\perp} = (k_{\rm B}T/4\pi\eta_0 L)(s - r_{\perp}) \tag{20}$$

$$D_{\rm R} = (3k_{\rm B}T/(\pi\eta_0 L^3))(s - \zeta) \tag{21}$$

where

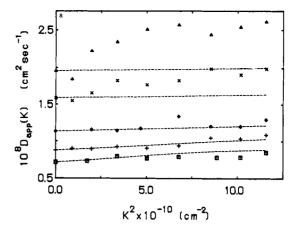
$$s = \ln \left(2L/d \right) \tag{22}$$

$$r_{\parallel} = 1.27 - 7.4((1/s) - 0.34)^2 \tag{23}$$

$$r_{\perp} = 0.19 - 4.2((1/s) - 0.39)^2$$
 (24)

$$\zeta = 1.45 - 7.5(1/s - 0.27)^2 \tag{25}$$

The angular dependence of $D_{\rm app}(C=0,K)$ can be calculated from eq 18 and is represented in parts a and b of Figure 6 by the dashed line for five PPTA samples in 96% H₂SO₄ and 96% H₂SO₄ + 0.05 M K₂SO₄, respectively. The agreement between the experimentally measured points and the dashed curve appears to be fair for high molecular weight samples; but the disparity is obvious for the lower molecular weight samples. $\bar{D}_z^0(C=0,K=0) = 0.88 \times 10^{-8}$ cm²/s for sample 4 in Figure 6a, as listed in Table I, while



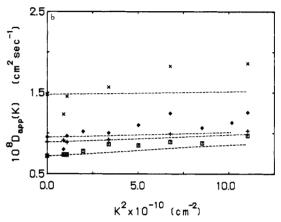


Figure 6. (a) Plots of $D_{\rm app}(K) = (\bar{\Gamma}(0,K)/K^2)$ vs. K^2 for PPTA in 96% $H_2{\rm SO}_4$. Dashed lines are calculated from Schurr's equation, eq 18. (\square) sample 5; (+) sample 4; (\blacklozenge) sample 3; (×) sample 2; (A) sample 1. (b) Plots of $D_{\rm app}(K) = (\overline{\Gamma}(0,K)/K^2)$ vs. K^2 for PPTA in 96% $H_2{\rm SO}_4 + 0.05$ M $K_2{\rm SO}_4$. Dashed lines are calculated from Schurr's equation 18. (a) sample 5; (+) sample 4; (\blacklozenge) sample 3; (\times) sample 2.

Table II Average Persistence Length per Chain (L_w/ρ) of PPTA in 96% H2SO4 with and without Added Salta

sample	solvent	$M_{\rm w} \times 10^{-4}$	$L_{\mathbf{w}}$,	T /.
sample	Solvelit	10 -	nm	$L_{\mathbf{w}}/\rho$
5	96 wt % H ₂ SO ₄	4.83	256	9
4	96 wt % H ₂ SO ₄	3.84	203	7
3	96 wt % H ₂ SO ₄	2.27	120	4
2	96 wt % H ₂ SO ₄	1.59	84	3
1	96 wt % H ₂ SO ₄	1.45	77	3
5	96 wt % H ₂ SO ₄ + 0.005 M K ₂ SO ₄	4.42	234	12
4	96 wt % H ₂ SO ₄ + 0.005 M K ₂ SO ₄	3.03	160	8
5	96 wt % $H_2SO_4 + 0.05 \text{ M K}_2SO_4$	4.26	226	11
4	96 wt % $H_2SO_4 + 0.05 \text{ M K}_2SO_4$	2.98	158	8

 $^{a}L_{w} = (M_{w}/M_{o}) \times l_{o} = (M_{w}/238) \times 1.26 \text{ nm}; \rho = 29\text{-nm persist-}$ ence length of PPTA in 96% H_2SO_4 ; $\rho = 20$ -nm persistence length of PPTA in 96% $H_2SO_4 + (0.05 \text{ or } 0.005 \text{ M}) K_2 \hat{S}O_4$.

 \bar{D}_z^0 [$\equiv \lim_{C \to 0, K \to 0} \bar{\Gamma}/K^2$] = 0.86×10⁻⁸ cm²/s according to Figure 1a.

The Wilcoxon-Schurr eq 18 for rigid rods cannot be expected to hold for semiflexible chains. Table II lists the average number of persistence lengths per chain $(L_{\rm w}/\rho)$ of the PPTA samples we have investigated. The angular dependence of $D_{app}(C=0,K)$ can be represented by eq 11 in a semilogarithmic plot where we have been able to evaluate f, a dimensionless parameter defined by Stockmayer and Schmidt,⁹ from the slopes and values of $\langle R_g^2 \rangle_{app}$ according to eq 11, as listed in Table I. For unfractionated

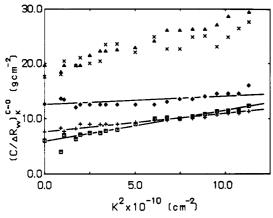


Figure 7. Plots of $(C/\Delta R_{\rm vv})_{\rm K}^{C=0}$ vs. K^2 for PPTA (samples 1-5) in 96% H₂SO₄: (\square) sample 5; (+) sample 4; (\triangle) sample 3; (×) sample 2; (\blacklozenge) sample 1. $R_{\rm g}$ values for samples 3-5 are listed in Table I.

PPTA samples with weight-average molecular weights varying from 2 × 10⁴ to 5 × 10⁴, $f \sim 0.2$ –0.3 for $L_{\rm w}/2\rho$ ranging from 2 to 4.4, where $L_{\rm w} = N_{\rm w} l_0$ with repeating unit length $l_0 = 12.6$ Å and $N_{\rm w} = M_{\rm w}/238$ for PPTA assuming that $\rho = 290$ Å.

The concentration and angular dependence of $D_{\rm app}(C,\!K)$ can be expressed finally by

$$\ln \left(\bar{\Gamma}(C,K)/K^2 \right) =$$

$$\ln (\bar{\Gamma}(0,0)/K^2) + \ln (1 + k_d C) + F*K^2$$
 (26)

where $F^* = f\langle R_g^2(C) \rangle_{app} \ (\equiv f\xi^2$, with ξ being the correlation length) and we have taken $\ln (1 + F^*K^2) \simeq F^*K^2$. As C approaches zero

$$\ln \left(\bar{\Gamma}(0,K)/K^2\right) = \ln \left(\bar{\Gamma}(0,0)/K^2\right) + F_0 * K^2$$
 (27)

where we have taken F_0^* to be the value of F^* at infinite dilution. The change of F^* with respect to concentration comes mainly from the effective size change with respect to concentration. As K approaches zero

$$(\bar{\Gamma}(C,0)/K^2) = (\bar{\Gamma}(0,0)/K^2) + k_d*(K=0)C$$
 (28)

Thus, the term $(\bar{\Gamma}(0,0)/K^2)$ can be evaluated from plots of $(\bar{\Gamma}(C,K)/K^2)$ vs. concentration and scattering angle according to eq 27 and 28, similar to the Zimm plot used in static LS data analysis, as shown in Figure 7.

III. Overlap Threshold between Dilute and Semidilute Solution Regimes

According to the scaling theory for athermal polymer solutions, the osmotic pressure is related to C/C^{*} at constant temperature T as

$$(\Pi/T) = (C/N)f(C/C^*)$$
(29)

where C is the concentration; N, the degree of polymerization; and C^* , the overlap threshold concentration from dilute to semidilute solutions. In dilute solution $f(C/C^*)$ is expressed as

$$f(C/C^*) = 1 + B(C/C^*) + \dots$$
 (30)

where B is a constant. According to eq 29 and 30, we have

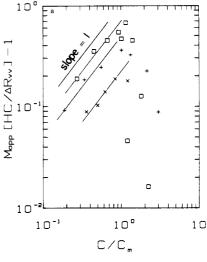
$$\Pi/T = (C/N)[1 + B(C/C^*) + \dots]$$
 (31)

Then the osmotic compressibility $(\Delta\Pi/\Delta C)_{T,P}$ at constant temperature T and pressure P has the form

$$(N/T)(\partial \Pi/\partial C)_{T,P} = 1 + 2B(C/C^*)$$

or

$$\log \left[(N/T)(\partial \Pi/\partial C) - 1 \right] = \log \left(\text{constant} \right) + \log \left(C/C^* \right)$$



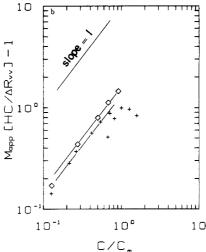
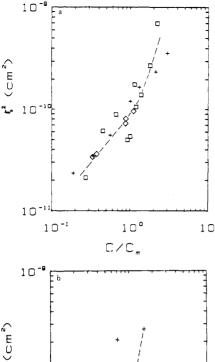


Figure 8. (a) Plots of log $[M_{\rm app}(HC/\Delta R_{\rm vv})-1]$ vs. log $(C/C_{\rm m})$ for PPTA in 96% $\rm H_2SO_4$: (a) sample 5; (+) sample 4; (×) sample 2. (b) Plots of log $[M_{\rm app}(HC/\Delta R_{\rm vv})-1]$ vs. log $(C/C_{\rm m})$ for PPTA (sample 4) in 96% $\rm H_2SO_4+0.05~M~K_2SO_4$ (\$\darphi\$) and 96% $\rm H_2SO_4+0.005~M~K_2SO_4$ (\$\darphi\$).

where we have dropped the subscripts T and P for the osmotic compressibility. In a plot of $\log [(N/T)(\partial \Pi/\partial C) - 1]$ vs. $\log (C/C^*)$ the slope is equal to 1 in the dilute solution regime.

In a previous paper² we report a minimum value for $\Delta R_{\rm vv}/(HC)$ occurring at concentration $C_{\rm m}$ in a plot of $\Delta R_{\rm vv}/(HC)$ vs. concentration at constant molecular weight. Parts a and b of Figure 8 show plots of $\log [M_{\rm app}(HC/\Delta R_{\rm vv})-1]$ vs. $\log (C/C_{\rm m})$ for PPTA in 96% $H_2{\rm SO}_4$ and 96% $H_2{\rm SO}_4+0.05$ M (or 0.005 M) $K_2{\rm SO}_4$, where $M_{\rm app}$ is the apparent molecular weight. In the concentration region $C < C_{\rm m}$, the slopes for all three PPTA samples are close to one, indicating dilute solution behavior. Small deviations in slope (≈ 1) appear to occur for $C \lesssim C_{\rm m}$. For $C > C_{\rm m}$, $\log [(M_{\rm app})(HC/\Delta R_{\rm vv})-1]$ drops down sharply with increasing concentration, and the decrease does not appear to correlate with molecular weight. The results suggest that for wormlike chains, the dilute solution behavior covers a concentration range much greater than $M/(N_{\rm A}L^3)$.

covers a concentration range much greater than $M/(N_{\rm A}L^3)$. The correlation length ξ [= $\langle R_{\rm g}^{\ 2}(C)\rangle_{\rm app}^{\ 1/2}$] equivalent to the apparent root mean square radius of gyration at finite concentration C is influenced by interactions among chains. In a double-logarithmic plot, parts a and b of Figure 9 show ξ^2 as a function of $C/C_{\rm m}$ for PPTA in ${\rm H_2SO_4}$ and ${\rm H_2SO_4}$ + 0.05 M ${\rm K_2SO_4}$, respectively. ξ^2 increases with increasing $C/C_{\rm m}$ up to $C=C_{\rm m}$; beyond $C_{\rm m}$ the slope appears to in-



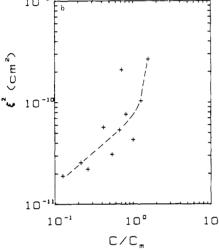


Figure 9. (a) log-log plots of ξ^2 vs. $C/C_{\rm m}$ for PPTA sample 5, (\square), sample 4 (+), and sample 3 (\diamond) in 96% H₂SO₄. The dashed curve is used to suggest the appearance of an increasing slope for $C>C_{\rm m}$. (b) log-log plots of ξ^2 vs. $C/C_{\rm m}$ for PPTA sample 4 in 96% H₂SO₄ + 0.005 M K₂SO₄. The dashed curve is used to suggest the appearance of an increasing slope for $C>C_{\rm m}$.

crease even more sharply for PPTA in 96% $\rm H_2SO_4$ with and without added salt, similar to the observations made by Burchard for aqueous poly(vinylpyrrolidone) solutions in semidilute solutions.⁶ Interchain association could be one possible reason for this additional increase as well as the curvature noted at high concentrations in Figure 1. However, we have no experimental evidence to prove the actual causes for the additional changes. Doi and Edwards¹⁰ have shown that the overlap concentration for rigid rods $C^{**} < M/(N_A dL^2)$. With $M_{\rm w} = M_0 N_{\rm w}$ and $L = l_0 N_{\rm w}$, the inequality can be rewritten as

$$C^{**} < M_0/(N_A dl_0 L) \text{ (g/cm}^3)$$
 (33)

where M_0 and l_0 are the weight and the length of each repeating unit. According to the inequality (33), C^{**} is proportional to the reciprocal of contour length L.

From our experimental results, we clearly see the dilute solution behavior at $C < C_{\rm m}$. Beyond $C_{\rm m}$, the solution behavior is correlated to the macromolecular size and changes sharply with increasing concentration. Thus, it is perhaps more reasonable to regard $C_{\rm m}$ as the overlap threshold concentration from the semidilute to the concentrated solution regime. Values of $C_{\rm m}$ (expressed in $\rm g/cm^3$) for four PPTA samples with different molecular weights are listed in Table III. Within our experimental error limits, $C_{\rm m}$ appears to be relatively independent of

Table III Crossover Concentration of Rodlike Polymers in Solution

		$C_{\rm m} \times 10^{-3}$, g/cm ³		
sample	solvent	obsd	comput- ed ^a	$C^{**} \times 10^{-3}$, $^{b} \text{ g/cm}^{3}$
5	96 wt % H ₂ SO ₄	2.5	2.5	2.0
4	96 wt % H ₂ SO ₄	2.1	2.7	2.6
2	96 wt % H ₂ SO ₄	1.8	3.4	6.2
1	96 wt % H ₂ SO ₄	2.4	3.4	6.8
4	96 wt % H ₂ SO ₄ + 0.005 M K ₂ SO ₄	~4	~3.8	
4	96 wt $\%$ $H_2SO_4 + 0.05$ M K_2SO_4	~4.5	~3.8	

 $^{a}C_{\rm m}=B^{*}[M_{\rm w}/[N_{\rm A}(L/\rho)^{1/4}d\rho L]\}~{\rm g/cm^{3}},~{\rm where}~B^{*}\sim0.24,~\rho=29{\rm -nm}~{\rm persistence}~{\rm length}~{\rm of}~{\rm PPTA}~{\rm in}~96\%~{\rm H_{2}SO_{4}},~{\rm and}~\rho\sim20{\rm -nm}~{\rm persistence}~{\rm length}~{\rm of}~{\rm PPTA}~{\rm in}~96\%~{\rm H_{2}SO_{4}}+(0.05~{\rm or}~0.005~{\rm M})~{\rm K_{2}SO_{4}}.~^{b}C^{**}=M_{o}/(N_{\rm A}dl_{o}L)~{\rm g/cm^{3}}.$

molecular weight. Consequently, we view the crossover behavior for wormlike chains (PPTA in concentrated sulfuric acid) with a modified perspective. Rodlike polymers are prone to interchain association.4 The effect of association is expected to occur in semidilute solutions where macromolecules are more likely to have contact with one another. On the other hand, the probability for macromolecules to be associated with one another is proportional to the macromolecular chain rigidity. The shorter chains are more rigid and are easier to be associated with one another. Therefore, if we take $C_{\rm m}$ as the concentration at which macromolecules touch one another, the magnitude of $C_{\rm m}$ can be expected to be influenced by both macromolecular size and chain rigidity. We define 12 an effective length L^* , which is related to the contour length L, and an effective diameter d^* .

$$L^* = (\rho L)^{1/2} \tag{34}$$

$$d^* = (L/\rho)^{1/4}d\tag{35}$$

where we have assumed the molecular volume of a semi-flexible chain to be independent of chain flexibility. Then for C_{m} , a similar inequality can be written as

$$C_{\rm m} < M/(N_{\rm A}d^*L^{*2})$$
 (36)

or

$$C_{\rm m} \sim B*M/(N_{\rm A}d*L*^2)$$
 (37)

For rigid rods, the persistence length is L; we then retrieve eq 36 or

$$C_{\rm m} < M_0 / (N_{\rm A} dl_0 L) \tag{38}$$

which is the same as the Doi–Edwards inequality for C^{**} . For wormlike chains, ρ is shorter than the contour length L and thus $L^* < L$. In Table II, our data show that $C_{\rm m}$ for PPTA in concentrated sulfuric acid with added salt appears to have a higher value than the one without added salt, corresponding to the fact that PPTA in concentrated sulfuric acid has a higher persistence length than those with added salt. The experimental data for $C_{\rm m}$ and the results calculated from eq 38 with an adjustable parameter $B^* \sim 0.24$ and a persistence length $\rho = 290$ and 200 Å for PPTA in 96% H_2SO_4 and in $H_2SO_4 + 0.005$ M K_2SO_4 , respectively, are in fairly good agreement. The introduction of effective L^* and d^* to take into account chain flexibility seems to retain, at least qualitatively, the crossover behavior from dilute to semidilute and from semidilute to concentrated solutions for wormlike chains.

In summary, we have found that by using a semilogarithmic relationship, $\log \bar{\Gamma}(K)/K^2$ vs. K^2 , $\bar{\Gamma}$ can be ex-

trapolated to zero scattering angle with more confidence. The translational diffusion coefficient at infinite dilution can be evaluated by using a modified Zimm plot (eq 27 and 28). We observed dilute solution behavior at $C < C_{\rm m}$, at which concentration $[\Delta R_{\rm vv}/(HC)]$ also shows a minimum. The concentration $C_{\rm m}$ $[\sim M/(N_{\rm A}d^*L^{*2})]$ differs from C^{**} $[\sim M/(N_{\rm A}dL^2)]$ for rigid rods. The solution behavior for semiflexible chains is correlated to the macromolecular size and changes sharply with increasing concentration (Figure 9). Thus, we consider it more reasonable to regard $C_{\rm m}$ as the threshold concentration from the semidilute to the concentrated solution regime. Furthermore, for wormlike chains, the concentration range between semidilute and concentrated solution regimes is more compressed.

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Registry No. PPTA (SRU), 24938-64-5; PPTA (copolymer), 25035-37-4; K₂SO₄, 7778-80-5.

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Application of Raman and Laser Light Scattering to the Melt Polymerization of Hexachlorocyclotriphosphazene. 1

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ABSTRACT: The application of a novel laser light scattering apparatus is described for on-line monitoring of the high-temperature, melt polymerization of hexachlorocyclotriphosphazene (HCTP) and the in situ characterization of the poly(dichlorophosphazene) (PDP) product. A combination of Raman spectroscopy, angular measurement of absolute light scattering intensities, and Rayleigh line width (dynamic) light scattering measurements are employed. More conventional techniques are inappropriate due to the polymer's hydrolytic instability, the high temperature required for polymerization, and the nature and apparent complexity of the reaction. Concentrations of the reaction components and characteristics of the polymer, such as weight-average molecular weight (M_w) and z-average radius of gyration (R_g) in the dilute solution regime and the cooperative diffusion coefficient (D_c) and osmotic compressibility $[(\tilde{\partial}\Pi/\partial C)_{TP}]$ in semidilute solutions, are monitored with polymerization time. Experimental results are found to be in excellent agreement with those obtained indirectly by the batchwise polymerization of the same material.

Introduction

Poly(organophosphazenes) comprise a promising new class of technological polymers usually prepared by the organosubstitution of chlorine atoms on poly(dichlorophosphazene) (I). The precursor polymer I, a high molecular weight elastomer ($T_{\rm g}$, -63 °C), reacts with moisture and therefore must be modified in order to obtain long-term hydrolytic stability and other useful properties. Depending upon the size and nature of the side group substituents, polymers with a wide range of physical properties may be produced.

The polymer I is prepared by the high-temperature (ca. 250 °C) ring-opening polymerization of hexachlorocyclotriphosphazene (II).⁴ Polymerizations may be conducted in solution or in the cyclic trimer melt, and catalysts may

$$\begin{array}{c|c}
CI & P & N & P & CI \\
CI & || & | & CI & \Delta & -(N = PCI_2)_n - I \\
& & & & I
\end{array}$$

be employed to reduce the reaction temperature and control polymer structure.^{4,5} It is essential that II is highly pure and polymerization conditions are carefully controlled. If impurities are present or if the polymerization is allowed to continue too long or at too high a temperature, I may cross-link and thereby be unsuitable for organosubstitution.

The cyclic trimer II is a white crystalline (mp 112-114 °C) solid that sublimes under vacuum and is soluble in most organic solvents. The open-chain polymer I is soluble in a variety of solvents (e.g., benzene, trichlorobenzene, chloroform, and tetrahydrofuran) and typically has a high molecular weight $(M_{\rm w}=2\times10^6)$ and broad molecular weight distribution $(M_{\rm w}/M_{\rm n}=3-7)$. Precautions must be

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